

ML-DOCTOR: Holistic Risk Assessment of Inference Attacks Against Machine Learning Models

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Abstract

Inference attacks against Machine Learning (ML) models allow adversaries to learn information about training data, model parameters, etc. While researchers have studied these attacks thoroughly, they have done so in isolation. We lack a comprehensive picture of the risks caused by the attacks, such as the different scenarios they can be applied to, the common factors that influence their performance, the relationship among them, or the effectiveness of defense techniques. In this paper, we fill this gap by presenting a first-of-its-kind holistic risk assessment of different inference attacks against machine learning models. We concentrate on four attacks – namely, membership inference, model inversion, attribute inference, and model stealing – and establish a threat model taxonomy. Our extensive experimental evaluation conducted over five model architectures and four datasets shows that the complexity of the training dataset plays an important role with respect to the attack’s performance, while the effectiveness of model stealing and membership inference attacks are negatively correlated. We also show that defenses like DP-SGD and Knowledge Distillation can only hope to mitigate *some* of the inference attacks. Our analysis relies on a modular re-usable software, ML-DOCTOR, which enables ML model owners to assess the risks of deploying their models, and equally serves as a benchmark tool for researchers and practitioners.

1 Introduction

Over the last decade, research in Machine Learning (ML), and in particular Deep Learning, has made tremendous progress. Deployment and overall success of this technology are jeopardized by attacks against ML models, that prompt serious security and privacy risks. In particular, inference attacks [12, 18, 28, 34, 38, 43, 44, 46, 50, 51, 56] allow adversaries to infer information from a target ML model, e.g., about the training data, the model’s parameters, etc.

In this paper, we focus on four types of attacks: membership inference [46], model inversion [12], attribute inference [28], and model stealing [51]. The first three target a model’s *training dataset*, aiming to, respectively, determine whether or not an exact data sample belongs to it, recover

(part of) it, or predict properties that are not related to the model’s original task. Model stealing involves reconstructing the target model’s (non-public) parameters. Inference attacks can lead to severe consequences, violating individuals’ privacy, as ML models are often trained on sensitive data, or compromising the model owner’s intellectual property [10].

Overall, existing inference attacks have been studied under different threat models and experimental settings, albeit in isolation. This prompts the need for a holistic understanding of the risks caused by these attacks, such as the scenarios different inference attacks can be applied to, the common factors that influence these attacks’ performance, and the relations among the attacks, as well as the overall effectiveness of defense mechanisms.

1.1 Our Contributions

In this paper, we perform a first-of-its-kind holistic security and privacy risk assessment of ML models, vis-à-vis four representative inference attacks.

Threat Model Taxonomy. Our work starts with a systematic categorization of the knowledge that an adversary might have in order to launch inference attacks along two dimensions, i.e., access to: 1) a target model (white-box or black-box), 2) an auxiliary dataset (partial training dataset, shadow dataset, or no dataset). We consider four types of state-of-the-art inference attacks and describe under which threat models they can be applied to. This provides us with a full spectrum of inference attack surface for ML models.

Experimental Evaluation. We perform a comprehensive measurement study of the attacks, jointly, over five different ML model architectures (AlexNet [22], ResNet18 [17], VGG19 [47], Xception [8], and SimpleCNN) and four datasets (CelebA [27], Fashion-MNIST (FMNIST) [53], STL10 [9], and UTKFace [57]).

Main Findings. The complexity of the target model’s training dataset plays a major role in the accuracy of membership inference, model inversion, and model stealing. In particular, the former is much more effective on complex datasets, while the other two exhibit the opposite trend. For instance, the accuracy of membership inference (with black-box access to the target model and a shadow dataset) against ResNet18 is 0.88 for a more complex dataset such as STL10, while 0.54

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for a less complex one like FMNIST.¹ On the other hand, model stealing achieves 0.52 agreement (the standard metric for this attack) on ResNet18 trained on STL10 but a much higher 0.93 on FMNIST. This stems from ML models being more prone to overfitting on complex datasets, which leads to better membership inference. Whereas, when an ML model is trained on a complex dataset, it is harder for an adversary to obtain a dataset with similar complexity (by querying the target model) to train their stolen model.

We also find that the performance of membership inference and model stealing are negatively correlated ($r = -0.9$), i.e., a target model with higher membership risks is less vulnerable to model stealing. This is due to the opposite effect of overfitting on these two attacks. Moreover, we observe that access to a partial training dataset does not yield a significantly better attack performance for membership inference, attribute inference, and model stealing. For instance, the accuracy for attribute inference (on ResNet18/CelebA) is 0.72 with a partial training dataset, and 0.73 with a shadow dataset.

Defenses. We evaluate two defense mechanisms, i.e., DP-SGD [1] and Knowledge Distillation (KD) [20], against all the inference attacks. Empirical results show that DP-SGD can mitigate membership inference attacks in general without damaging target models’ utility significantly. Meanwhile, KD also reduces membership inference risks, but, generally, to a lesser extent compared to DP-SGD. However, neither of them are effective against other inference attacks. This highlights the lack of a general, effective defense mechanism, and our work sheds light as to what extent/why.

ML-DOCTOR. To support the comprehensive evaluation of a wide range of inference attacks and defenses (current and future), we introduce a framework called ML-DOCTOR. This can be used by multiple entities and for multiple purposes. For instance, model owners can use it to *meaningfully* assess potential security and privacy risks before deploying their model. Also, as we make source code publicly available, researchers will be able to re-use ML-DOCTOR to benchmark new inference attacks and defense mechanisms. Indeed, ML-DOCTOR follows a modular design, which easily supports the integration of additional inference attacks and defenses, as well as plugging in a variety of datasets, models, etc.

1.2 Paper Organization

The rest of the paper is organized as follows. In [Section 2](#), we present a taxonomy of threat models, then, introduce the attacks considered in this paper in [Section 3](#). Next, [Section 4](#) describes the design of ML-DOCTOR. In [Section 5](#), we introduce our experimental setup. Evaluation for attacks and defense mechanisms are presented in [Section 6](#) and [Section 7](#), respectively. We review related work in [Section 8](#) and conclude the paper in [Section 9](#).

¹We refer to both sample complexity and class diversity (see [Section 6.2](#)).

Auxiliary Dataset	Model Access	
	Black-Box (\mathcal{M}^B)	White-Box (\mathcal{M}^W)
Partial (\mathcal{D}_{aux}^P)	MemInf, ModSteal	MemInf, AttrInf
Shadow (\mathcal{D}_{aux}^S)	MemInf, ModSteal	MemInf, AttrInf, ModInv
No (\mathcal{D}_{aux}^N)	-	ModInv

Table 1: Different attacks under different threat models.

2 Threat Modeling

In this work, we focus on machine learning classification, one of the most popular ML applications. In general, the goal of an ML classifier is to map a data sample to a label/class. The input to an ML model is a data sample and the output is a vector of probabilities, or posteriors, with each element representing the likelihood of the sample belonging to a class.

We categorize the threat models for all inference attacks considered in this paper along two dimensions, i.e., 1) *access to the target model* and 2) *auxiliary dataset*. In total, we consider five different scenarios.

Access to the Target Model. We consider two access settings: *white-box* and *black-box*. The former, denoted with \mathcal{M}^W , means that an adversary has full information about the target model, including its parameters and architecture. In black-box attacks, denoted with \mathcal{M}^B , the adversary can only access the target model in an API-like manner, e.g., they can query the target model and get the model’s output. However, most of the existing black-box literature [14, 46, 54] also assumes that the adversary knows the target model’s architecture which they use to build shadow models (see [Section 3](#)).

Overall, the white-box model captures scenarios where the target model’s parameters are leaked, e.g., following a data breach or through reverse engineering, e.g., from pre-trained models deployed to mobile devices [20]. Whereas, the black-box model encapsulate API access akin to features provided by Machine Learning as a Service (MLaaS) platforms.

Auxiliary Dataset. The adversary needs an auxiliary dataset in order to train their attack model. We consider three scenarios, in decreasing order of adversarial “strength”: 1) *partial training dataset* (\mathcal{D}_{aux}^P), 2) *shadow dataset* (\mathcal{D}_{aux}^S), and 3) *no dataset* (\mathcal{D}_{aux}^N). In the first scenario, the adversary obtains parts of the actual training data from the target model (e.g., it is public knowledge), while in the last one, they have no information at all. In between is the \mathcal{D}_{aux}^S setting, where the adversary gets a “shadow” dataset from the same distribution as the target model’s training data (see [Section V-C](#) in [46] for a discussion on how to generate such data, using, e.g., through model-based or statistics-based synthesis, or noisy real data).

Considered Settings. Overall, the two different types of model access and the three types of auxiliary dataset availability lead to six threat models. In the rest of the paper, we consider five of them: $\langle \mathcal{M}^B, \mathcal{D}_{aux}^P \rangle$, $\langle \mathcal{M}^B, \mathcal{D}_{aux}^S \rangle$, $\langle \mathcal{M}^W, \mathcal{D}_{aux}^P \rangle$, $\langle \mathcal{M}^W, \mathcal{D}_{aux}^S \rangle$, and $\langle \mathcal{M}^W, \mathcal{D}_{aux}^N \rangle$. We do not experiment with black-box access and no auxiliary dataset, as this is unlikely to yield successful attacks.

3 Inference Attacks

In this section, we present the four inference attacks measured in this paper. Specifically, we consider: membership inference (MemInf), model inversion (ModInv), attribute inference (AttrInf), and model stealing (ModSteal). The first three are designed to infer information about a target ML model’s training data, while the last one aims to steal the target model’s parameters.

Different attacks can be applied to different threat models, as summarized in Table 1. For each attack and each threat model, we concentrate on one representative state-of-the-art method.

3.1 Membership Inference

Membership Inference (MemInf) [46] against ML models involves an adversary aiming to determine whether or not a target data sample was used to train a target ML model. More formally, given a target data sample x_{target} , (the access to) a target model \mathcal{M} , and an auxiliary dataset \mathcal{D}_{aux} , a membership inference attack can be defined as:

$$\text{MemInf} : x_{\text{target}}, \mathcal{M}, \mathcal{D}_{\text{aux}} \rightarrow \{\text{member}, \text{non-member}\}$$

where $\mathcal{M} \in \{\mathcal{M}^{\text{B}}, \mathcal{M}^{\text{W}}\}$ and $\mathcal{D}_{\text{aux}} \in \{\mathcal{D}_{\text{aux}}^{\text{P}}, \mathcal{D}_{\text{aux}}^{\text{S}}\}$.

Membership inference has been extensively studied in literature [6, 7, 21, 23, 25, 30, 42, 44, 46]. Inferring membership of a target sample prompts severe privacy threats; for instance, if an ML model for drug dose prediction is trained using data from patients with a certain disease, then inclusion in the training set inherently leaks the individuals’ health status. Overall, MemInf is also often a signal that a target model is “leaky” and can be a gateway to additional attacks [10].

In the following, we illustrate how to implement membership inference (MemInf) under different threat models.

Black-Box/Shadow $\langle \text{MemInf}, \mathcal{M}^{\text{B}}, \mathcal{D}_{\text{aux}}^{\text{S}} \rangle$ [44]. We start with the most common and difficult setting for the attack [44, 46], whereby the adversary has black-box access (\mathcal{M}^{B}) to the target model and a shadow auxiliary dataset ($\mathcal{D}_{\text{aux}}^{\text{S}}$).

The adversary first splits the shadow dataset into two parts and uses one to train a shadow model on the same task. Next, the adversary uses the entire shadow dataset to query the shadow model. For each querying sample, the shadow model returns its posteriors and the predicted label: if the sample is part of the shadow model’s training set, the adversary labels it as a member, and as a non-member otherwise. With this labeled dataset, the adversary trains an attack model, which is a binary membership classifier. Finally, to determine whether a data sample is a member of the target model’s training dataset, the sample is fed to the target model, and the posteriors and the predicted label (transformed to a binary indicator on whether the prediction is correct) are fed to the attack model.

Black-Box/Partial $\langle \text{MemInf}, \mathcal{M}^{\text{B}}, \mathcal{D}_{\text{aux}}^{\text{P}} \rangle$ [44]. If the adversary has black-box access to the target model and a partial training dataset, the attack method is very similar to that for $\langle \text{MemInf}, \mathcal{M}^{\text{B}}, \mathcal{D}_{\text{aux}}^{\text{S}} \rangle$. However, the adversary does not need to train a shadow model; rather, they use the partial training

dataset as the ground truth for membership and directly train their attack model.

White-Box/Shadow $\langle \text{MemInf}, \mathcal{M}^{\text{W}}, \mathcal{D}_{\text{aux}}^{\text{S}} \rangle$ [31]. Nasr et al. [31] introduce an attack in the white-box setting with either a shadow or a partial training dataset as the auxiliary dataset.² In the former, similar to $\langle \text{MemInf}, \mathcal{M}^{\text{B}}, \mathcal{D}_{\text{aux}}^{\text{S}} \rangle$, the adversary uses $\mathcal{D}_{\text{aux}}^{\text{S}}$ to train a shadow model to mimic the behavior of the target model and to generate data to train their attack model. As the adversary has white-box access to the target model, they can also exploit the target sample’s gradients with respect to the model parameters, embeddings from different intermediate layers, classification loss, and prediction posteriors (and label).

White-Box/Partial $\langle \text{MemInf}, \mathcal{M}^{\text{W}}, \mathcal{D}_{\text{aux}}^{\text{P}} \rangle$ [31]. The attack methodology here is almost identical to the black-box counterpart. The only difference is that the adversary can use the same set of features as the attack model for $\langle \text{MemInf}, \mathcal{M}^{\text{W}}, \mathcal{D}_{\text{aux}}^{\text{S}} \rangle$.

3.2 Model Inversion

Model inversion attacks (ModInv) [12] aim to reconstruct data samples from a target ML model, i.e., they allow an adversary to directly learn information about the training dataset.

For instance, in a facial recognition system, a ModInv adversary tries to learn the facial data of a victim whose data is used to train the model. Model inversion requires the adversary to have white-box access to the target model, this is due to the fact that the attack needs to perform back-propagation over the target model’s parameters (detailed below).

Formally, we define model inversion as:

$$\text{ModInv} : \mathcal{M}^{\text{W}}, \mathcal{D}_{\text{aux}} \rightarrow \{\text{training samples}\}$$

where $\mathcal{D}_{\text{aux}} \in \{\mathcal{D}_{\text{aux}}^{\text{N}}, \mathcal{D}_{\text{aux}}^{\text{S}}\}$.

We consider two types of model inversion attacks: the one proposed by Fredrikson et al. [12], which aims to reconstruct a representative sample for each class of the target model, and that by Zhang et al. [56], which aims to synthesize the training dataset. These two attacks follow different threat models, which we discuss next.

White-Box/No Auxiliary $\langle \text{ModInv}, \mathcal{M}^{\text{W}}, \mathcal{D}_{\text{aux}}^{\text{N}} \rangle$ [12]. The method by Fredrikson et al. [12] assumes the adversary has white-box access to the target model³ and does not need any auxiliary dataset. For each class of the target model, the adversary first creates a noise sample, feeds this sample to the model, and gets the posteriors. The adversary then uses back-propagation over the target model’s parameters to optimize the input sample so that the corresponding posterior of the class can exceed a pre-set threshold. Once the threshold is reached, the optimized sample is the representative sample of that class, i.e., the attack output.

White-Box/Shadow $\langle \text{ModInv}, \mathcal{M}^{\text{W}}, \mathcal{D}_{\text{aux}}^{\text{S}} \rangle$ [56]. The attack by Zhang et al. [56] uses a shadow dataset to enhance the

²The attack by Nasr et al. [31] was originally designed for the partial training dataset setting but it can be adapted to the shadow dataset setting.

³Fredrikson et al. [12] also introduce a model inversion attack where the adversary only has black-box access to the target model, however, its performance is not as good and therefore we do not consider it.

quality of the reconstructed samples by training a generative adversarial network (GAN) [15]. First, the adversary trains a GAN with a shadow dataset. Next, the adversary optimizes the inputs to the GAN’s generator, i.e., the noise, to find those GAN-generated samples that can achieve high posteriors on the target model. These samples are the attack’s final outputs. In other words, this attack performs optimization on the inputs to the GAN, instead of the samples to the target model directly [12]. Since the GAN is capable of generating high-quality samples, the attack’s final outputs will be more realistic. Moreover, due to the fact that GAN can generate multiple samples, this attack is able to generate multiple samples for each class of the target model as well.

3.3 Attribute Inference

An ML model may learn extra information about the training data that is not related to its original task; e.g., a model predicting age from profile photos can also learn to predict race [28, 50]. Attribute inference (AttrInf) aims to exploit such unintended information leakage.

State-of-the-art attacks usually rely on the embeddings of a target sample (x_{target}) obtained from the target model to predict the sample’s target attributes. Thus, the adversary is assumed to have white-box access to the target model. Formally, attribute inference is defined as:

$$\text{AttrInf} : x_{\text{target}}, \mathcal{M}^W, \mathcal{D}_{\text{aux}} \rightarrow \{\text{target attributes}\}$$

where $\mathcal{D}_{\text{aux}} \in \{\mathcal{D}_{\text{aux}}^P, \mathcal{D}_{\text{aux}}^S\}$ can either be a partial training dataset or a shadow dataset.

White-Box/Shadow and Partial [28, 50]. Both attacks, i.e., $\langle \text{AttrInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$ [28] and $\langle \text{AttrInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^P \rangle$ [50], follow a similar attack methodology. The only difference lies in the dataset used to train the attack model. In both cases, the adversary is assumed to know the target attributes of the auxiliary dataset. Then, they use the embeddings and the target attributes to train a classifier to mount the attack.

3.4 Model Stealing

The goal of model stealing attacks (ModSteal) [34, 51], aka model extraction, is to extract the parameters from a target model. Ideally, an adversary will be able to obtain a model (the “stolen” model) with very similar performance as the target model. More formally:

$$\text{ModSteal} : \mathcal{M}^B, \mathcal{D}_{\text{aux}} \rightarrow \mathcal{M}^C$$

where \mathcal{M}^C is the stolen model and $\mathcal{D}_{\text{aux}} \in \{\mathcal{D}_{\text{aux}}^P, \mathcal{D}_{\text{aux}}^S\}$.

Model stealing prompts severe security risks. For instance, as it is often difficult to train an advanced ML model (e.g., due to the lack of data or computing resources), stealing a trained model inherently constitutes intellectual property theft. Also, as many other attacks, such as adversarial examples [39], require white-box access to the target ML model, model stealing can be a stepping stone to perform these attacks.

Black-Box/Partial and Shadow [51]. In this paper, we concentrate on the attacks proposed by Tramèr et al. [51], for

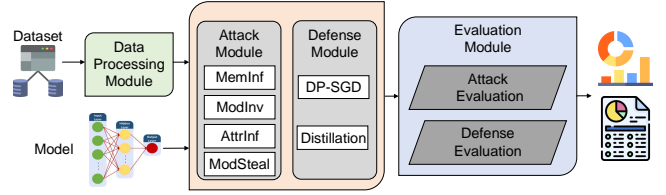


Figure 1: Overview of ML-DOCTOR’s modules.

$\langle \text{ModSteal}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^P \rangle$ and $\langle \text{ModSteal}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$. The adversary is assumed to have knowledge of the target model’s architecture, and both attacks follow a similar methodology. Specifically, the adversary uses data samples from their auxiliary dataset ($\mathcal{D}_{\text{aux}}^P$ or $\mathcal{D}_{\text{aux}}^S$) to query the target model and gets the corresponding posteriors. Then, they use them to train the stolen model, with the posteriors as the ground truth.

4 ML-DOCTOR

In this section, we introduce ML-DOCTOR, a modular framework geared to evaluate the four inference attacks, as well as the two defenses (see Section 7), considered in this paper.

Prior work has proposed software tools to evaluate attacks against ML models, such as adversarial examples [26, 37], backdoor attacks [35], and membership inference [29]. To the best of our knowledge, ML-DOCTOR is the first framework that jointly considers different types of inference attacks.

Modules. In Figure 1, we report the four different modules of ML-DOCTOR:

1. **Data Processing.** This processes the datasets to mount different attacks. It also involves data pre-processing, e.g., re-sizing and normalization, data partition, etc.
2. **Attack.** This module performs the actual inference attacks. At the moment, it supports ten different attacks belonging to four different attack types (see Section 3).
3. **Defense.** We currently support two representative mitigation techniques for inference attacks against ML models, as discussed later in Section 7.
4. **Evaluation.** This module is used to evaluate the performance of attacks and defenses.

The modular design of ML-DOCTOR allows to easily integrate additional attacks and defense mechanisms, as well as plugging in any dataset or model.

Using ML-DOCTOR. A user needs to submit their target model and its training dataset to use ML-DOCTOR. Here, the reason for submitting the training dataset is to achieve a full-fledged privacy risk assessment. We envision ML-DOCTOR to be used for the following purposes:

- As it supports a systematic taxonomy of different threat models for inference attacks, ML-DOCTOR enables model owners to obtain an overview of the threats their model may face when deployed in the real world.

- ML-DOCTOR provides a holistic assessment of different attacks, as well as the effectiveness of possible defenses. To our best knowledge, this is the first tool to provide such a comprehensive analysis of inference attacks.
- Researchers can re-use ML-DOCTOR as a benchmark tool to experiment with new inference attacks and defenses in the future.

NB: ML-DOCTOR is currently implemented in Python 3.8 and PyTorch 1.7.1. Complete source code of all modules can be obtained anonymously via the PC Chairs and will be made publicly available with the final version of the paper.

5 Experimental Settings

In this section, we present our experimental setup.

5.1 Datasets

For the sake of this paper, we experiment with four datasets:

- **CelebA** [27] contains 202,599 face images, each image is associated with 40 binary attributes. We select and combine 3 attributes out of 40 including *Heavy-Makeup*, *MouthSlightlyOpen*, and *Smiling* to form our target models' classes/labels. As each attribute is binary, this leads to an 8-class classification.
- **FMNIST (Fashion-MNIST)** [53] is also an image dataset with 70,000 grayscale images equally distributed among 10 different classes including T-shirt, trouser, pullover, dress, coat, sandal, shirt, sneaker, bag, and ankle boot.
- **STL10** [9] is a 10-class image dataset with each class containing 1,300 images. Classes include airplane, bird, car, cat, deer, dog, horse, monkey, ship, and truck.
- **UTKFace** [57] has 23,000 face images labeled with age, gender, and race. We only consider images from the largest four races in the dataset (White, Black, Asian, and Indian). This leaves us with 22,012 images.

Note that all the samples in the datasets are re-sized to 32×32 pixels. We randomly split each dataset into four equal parts:

1. **Target Training Dataset** is used to train all the target models, and to evaluate the performance of all membership inference attacks and both model inversion attacks. For attacks that require a partial training dataset, we sample 70% samples from the target training dataset.
2. **Target Testing Dataset** is used to evaluate the performance of the target model. It is also used to evaluate the performance of all membership inference, attribute inference, and model stealing attacks.
3. **Shadow Training Dataset** is used to train all the attacks that require a shadow dataset as the auxiliary dataset.

4. **Shadow Testing Dataset** is used to train two membership inference attacks that require a shadow dataset as the auxiliary dataset.

5.2 Attack Models

Membership Inference. Recall that there are four different scenarios for MemInf; we establish two types of attack models: one for the black-box and one for the white-box setting.

- **Black-box.** Our attack model has two inputs, the ranked target sample's posteriors and a binary indicator on whether the target sample being predicted correctly. Each input is first fed into a different 2-layer MLP (Multilayer Perceptron), then the two obtained embeddings are concatenated together, and fed into a 4-layer MLP.
- **White-box.** We have four inputs for this attack model, like the one used by Nasr et al. [31], including the target sample's posteriors, classification loss, gradients of the parameters of the target model's last layer, and one-hot encoding of its true label. Each input is fed into a different neural network structure and the resulted embeddings are concatenated together as one input to a 4-layer MLP.

We use ReLU as the activation function for the attack model. The mini-batch size is set to 64, and cross-entropy is the loss function. We use Adam as optimizer, with learning rate $1e-5$. The attack model is trained for 50 epochs. As the evaluation metric, we adopt *accuracy*, as done in previous work [44, 46].

Model Inversion. For the attack in [12], we set the threshold to 0.999, learning rate to $1e-2$, maximum iteration to 3,000, and early stop criteria to 100 for all the target models. This attack generates one representative sample for each class of the target model. Therefore, for all samples in one class, we first calculate their average sample, then get the mean-square error (MSE) between this averaged sample and the reconstructed sample by model inversion. Finally, we average the MSE value for all classes and use this as the evaluation metric.

For $\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$ [56], we first use the shadow training dataset to train a DC-GAN [41] with the noise of the generator set to 100. For the attack, we set the learning rate to $1e-3$, momentum to 0.9, lambda to 100, iteration round to 1,500, and clip range to 1. To evaluate the effectiveness of this attack, we use the same approach by Zhang et al. [56], i.e., we train an evaluation classifier on the identical task of the target model and use this evaluation classifier to see whether the reconstructed samples can be recognized correctly. We use the *accuracy* of this classifier on reconstructed samples as the performance metric.

Attribute Inference. We only use two datasets, namely, CelebA and UTKFace, to evaluate this attack as both of them have extra attributes for samples that can be used as the target attributes. For the former, we select two attributes: *Male* and *Young*. As mentioned before, each attribute is binary, thus, we have a total of 4 target attributes. For the latter, we choose *Male* and *Female* as the target attributes.

	CelebA	FMNIST	STL10	UTKFace
AlexNet	1.00 / 0.68	1.00 / 0.88	1.00 / 0.52	1.00 / 0.79
ResNet18	1.00 / 0.74	1.00 / 0.91	1.00 / 0.52	1.00 / 0.85
VGG19	1.00 / 0.73	1.00 / 0.91	1.00 / 0.59	1.00 / 0.83
Xception	1.00 / 0.74	1.00 / 0.92	1.00 / 0.57	1.00 / 0.84
SimpleCNN	1.00 / 0.71	1.00 / 0.90	1.00 / 0.52	1.00 / 0.82

Table 2: Performance of target models, namely, training/testing accuracy for each setting.

Our attack model is a 2-layer MLP, its input is the target sample’s embeddings from the second-to-last layer of the target model. We use cross-entropy as the loss function and Adam as the optimizer with learning rate 1e-3. The attack model is trained for 50 epochs. As the main evaluation metric, we use *accuracy* [50].

Model Stealing. We evaluate the model stealing attack over all 20 target models. For the stolen model, we use the same architecture as the target model [51]. Each stolen model is trained using the MSE loss and SGD as the optimizer (momentum 0.9 and learning rate 1e-2) for 50 epochs. *Agreement* is used to assess the success of the attack, calculating the proportion of samples in the target testing dataset on which the target and the stolen models make the same prediction.

5.3 Target Models

We focus on five model architectures including AlexNet [22], ResNet18 [17], VGG19 [47], Xception [8], and SimpleCNN (containing 2 convolutional layers and 2 fully connected layers) for all the four datasets introduced above. In total, we train 20 different target models.

For training, we set the mini-batch size to 64 and use cross-entropy as the loss function. We use stochastic gradient descent (SGD) as the optimizer with weight decay set to 5e-4 and momentum to 0.9. Each target model is trained for 300 epochs. The learning rate is 1e-2 before 50 epochs, 1e-3 from 50-100 epochs, and 1e-4 until the end. All target models’ training and testing accuracies are shown in Table 2.

6 Experimental Evaluation

In this section, we leverage ML-DOCTOR to provide a holistic assessment of inference attacks against ML models. We start with assessing the performance of the four attacks. We then analyze the impact of dataset and overfitting on attack performance, as well as the relation among different attacks.

Experiments are performed on an NVIDIA DGX-A100 Ubuntu 18.04 server. We report average results over five runs.

6.1 Attack Performance

Membership Inference. In Figure 2, we report the performance of MemInf. The attack achieves high accuracy on CelebA, STL10, and UTKFace. For instance, the attack accuracy of $\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$ on ResNet18 trained on the STL10 dataset is 0.93. However, the performance on FMNIST is not strong, as models trained on FMNIST generalize

well on non-member data samples—in other words, there is less overfitting [46] (see Section 6.3).

An adversary with white-box access to the target model generally achieves better performance than the one with black-box access. For instance, the accuracy of $\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$ is higher than that of $\langle \text{MemInf}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$, except for the FMNIST dataset on ResNet18, VGG19, and Xception. A similar observation can be drawn from $\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^P \rangle$ and $\langle \text{MemInf}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^P \rangle$; this is expected as the adversary can exploit more information in the white-box setting. In particular, we find that the classification loss possesses the strongest signal among others for the attack [31]. Meanwhile, partial training dataset also leads to better membership inference than the shadow dataset, however, the effect is less pronounced.

Model Inversion. Next, we measure the performance of the model inversion attacks; see Figure 3. As discussed in Section 5.2, we use different metrics to evaluate these two attacks, i.e., MSE for $\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$ and accuracy for $\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$, due to their different design. Thus, we cannot directly compare them. Rather, we evaluate their attack performance qualitatively (see Figure 4 for two examples), and discover that the images generated by $\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$ are more realistic than those by $\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^N \rangle$.⁴ This is due to the capability of GAN for generating high-quality samples.

Attribute Inference. The performance of the attribute inference attacks is shown in Figure 5. In general, the attacks work quite well. For instance, both $\langle \text{AttrInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$ and $\langle \text{AttrInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^P \rangle$ reach around 0.80 accuracy for ResNet18 trained on UTKFace. We also notice that using a partial training dataset does not provide the adversary with much advantage compared to using a shadow dataset. In some cases, partial training dataset even yields worse performance, as in the case of VGG19 trained on CelebA.

Model Stealing. Finally, we report the agreement metric to evaluate model stealing attacks; see Figure 6. Overall, ModSteal has strong performance. For instance, $\langle \text{ModSteal}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$ for ResNet18 trained on FMNIST achieves an agreement of 0.93. Similar to attribute inference, we observe that using a partial training dataset as the auxiliary dataset has lower performance than the shadow dataset for model stealing. One reason might be using partial training dataset querying the target model results in more confident posteriors (low entropy), which contain less information for the adversary to exploit.

6.2 The Role of the Datasets

We now explore the effect of dataset complexity on the attack performance; see Figure 7. (The x-axis represents the datasets and the y-axis shows the attack performance, and each node corresponds to one attack against one target model). Due to space limitations, we only show one plot for one threat model, for each attack.

⁴Similar results are shown by Zhang et al. [56].

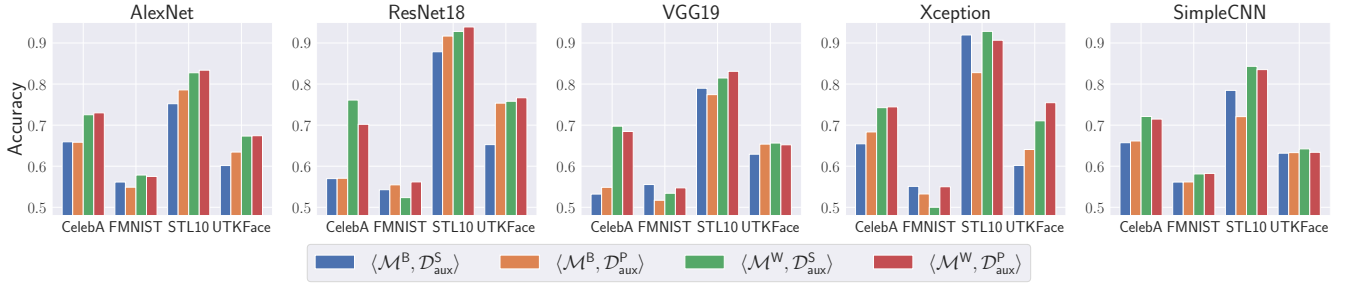


Figure 2: Performance of membership inference attacks (MemInf) under different threat models, datasets, and target model architectures.

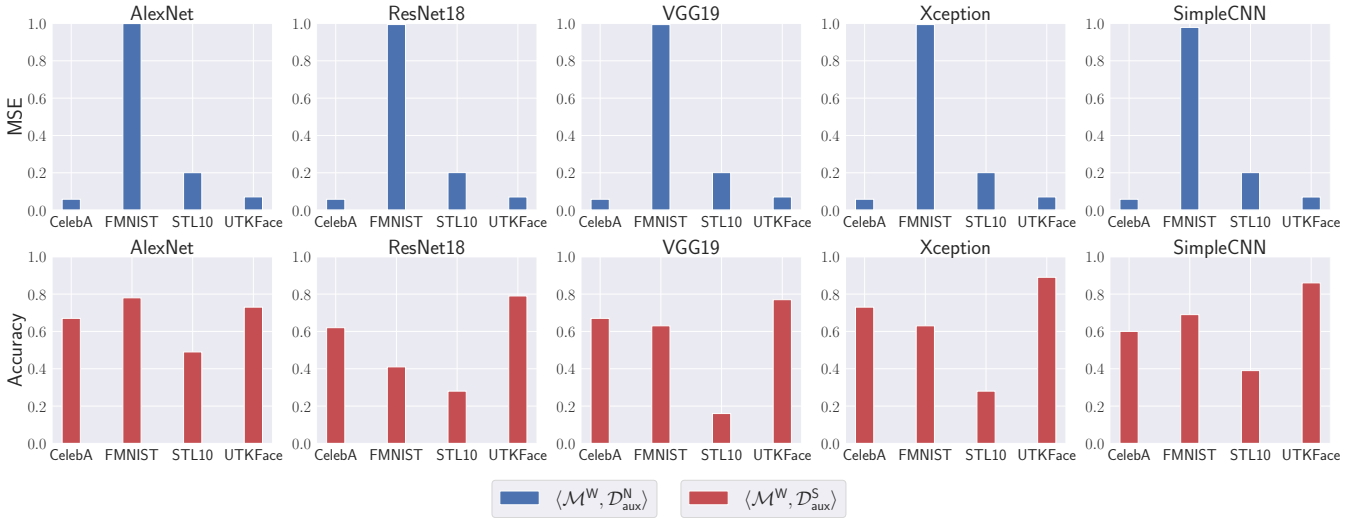


Figure 3: Performance of model inversion attacks (ModInv) under different threat models, datasets, and target model architectures.



Figure 4: Visualization of model inversion (AlexNet model trained on UTKFace). The left column depicts two samples reconstructed using [12], the middle one using [56], while the right column reports two samples from the target model’s training dataset.

Dataset Complexity. As mentioned before, all the samples in the four datasets are re-sized to 32×32 pixels. FMNIST is the simplest dataset as it only contains gray-scale images, followed by UTKFace, which consists of (full-color) human faces, and CelebA, which has 10 times more images than UTKFace. The most complex dataset is STL10, as it contains images of 10 diverse classes, ranging from cat to ship.

Results. Overall, the complexity of the dataset does have a significant effect on MemInf and ModSteal. More precisely, more complex datasets lead to better membership inference but worse model stealing performance. Ostensibly, this is due to the fact that a complex dataset is harder for a model to generalize on, and thus more prone to overfitting, which results in better membership inference attack [46]. Whereas, when a model is trained on a complex dataset, it is harder for an adversary to obtain a dataset with similar complexity (by querying the target model) to train their stolen model.

We also observe that model inversion is less effective on STL10 than on UTKFace and CelebA. Whereas, there is no strong influence of dataset complexity on attribute inference; this might due to the different target classes of our attacks on these two datasets (see Section 5.2). Note that we also investigate the complexity of the target model structure on the attack performance but do not observe any clear relation.

6.3 The Effect of Overfitting

Next, we analyze the effect of target models’ overfitting on inference attacks’ performance. We adopt two metrics to quantify overfitting in each target model: 1) the difference between the training accuracy and the testing accuracy of the target model, referred to as the *overfitting level*, and 2) the number of epochs used to train the target model [44].

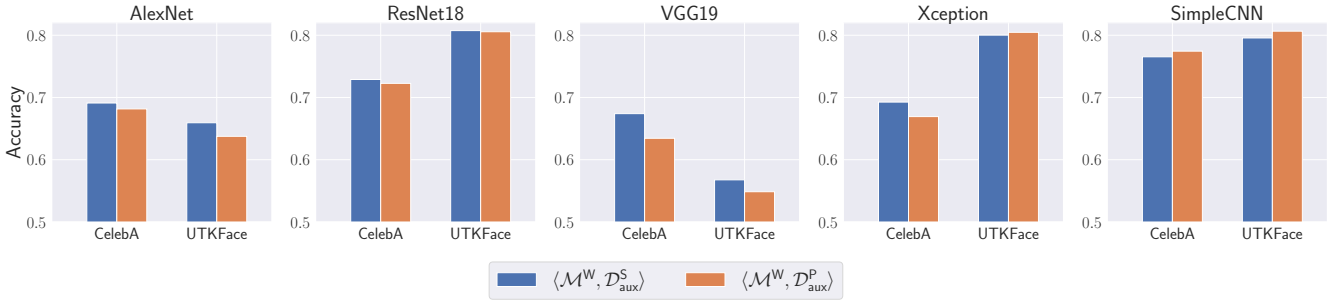


Figure 5: Performance of attribute inference attacks (AttrInf) under different threat models, datasets, and target model architectures.

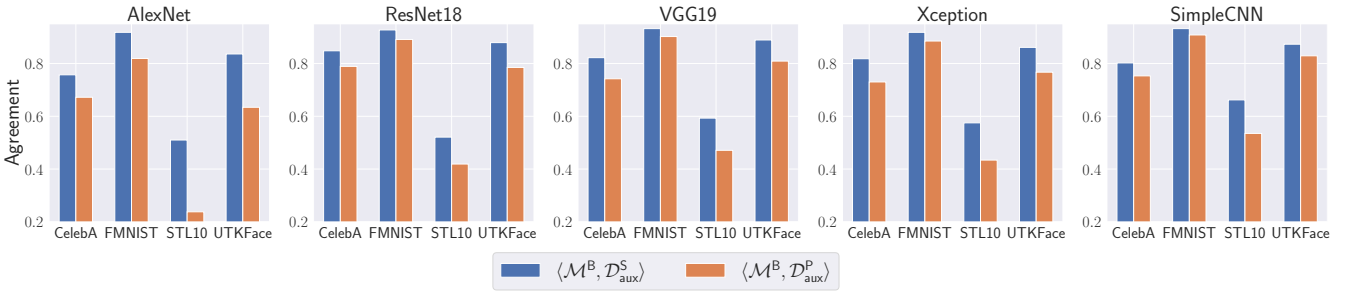


Figure 6: Performance of model stealing attacks (ModSteal) under different threat models, datasets, and target model architectures.

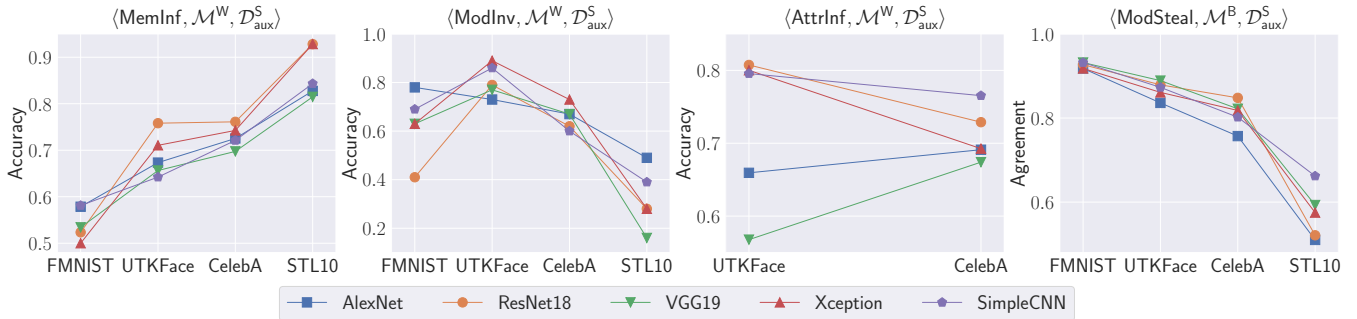


Figure 7: The relation between dataset complexity and attack performance.



Figure 8: The relation between overfitting level (on target models) and attack performance.

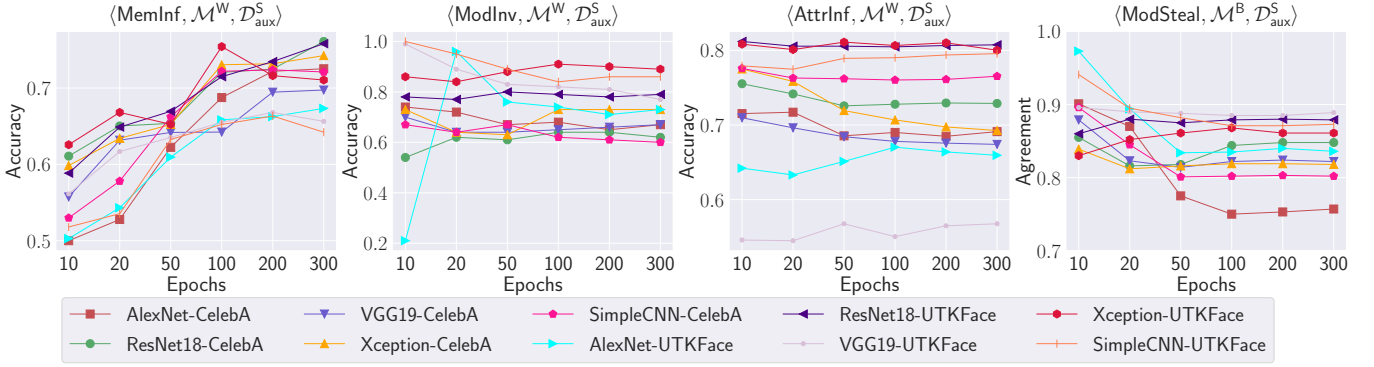


Figure 9: The relation between the number of epochs and attack performance.

Overfitting Level. The relation between overfitting level and attack performance is shown in Figure 8. First, we observe that different datasets have different overfitting levels, and this correlates well with the dataset complexity (see Section 6.2). Specifically, the largest (smallest) overfitting level happens on the most (least) complex dataset in our experiments, i.e., STL10 (FMNIST).

Overall, overfitting does have a significant impact on MemInf ($\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$). That is, a higher overfitting level leads to better membership inference. This is in line with previous analysis [44, 46], and is expected, as an overfitted model provides more confident predictions on its member samples (reflected on the posteriors) than on non-member samples, which can be exploited by the attack model to effectively differentiate them.

Meanwhile, model stealing displays a completely opposite trend, i.e., it is more difficult to steal a highly overfitted model. This can be explained by the fact that an overfitted model memorizes its training dataset to a large extent, and an adversary usually does not have the ability to get the exact training dataset, thus the stolen model is likely to be dissimilar to the target model. Also, model inversion tends to have better performance on less overfitted models, except for FMNIST. We believe this is due to the quality of the GAN employed in the attack model. For attribute inference, we do not observe a clear relationship between attack performance and overfitting level.

Number of Epochs. The relation between the number of epochs and attack performance (on UTKFace and CelebA) is shown in Figure 9. First, we find that all attacks’ performance becomes steady after 100 epochs; this is reasonable since 100 epochs are usually enough to train good target models, and further training does not cause an obvious effect on overfitting. Second, the performance of membership inference increases from 10 epochs until 100 epochs, while model stealing shows the opposite trend. This observation echoes our previous argument that a highly overfitted model is easier to be attacked by membership inference, but harder to be stolen. For model inversion and attribute inference, the attack performance only has slight fluctuations with a different number of epochs.

6.4 Relation Among Different Attacks

Next, we analyze the relationship between different attacks under the same threat model. In total, we consider all the six pairs of attacks (as depicted in Table 1) including MemInf and ModSteal under $\langle \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$, MemInf and ModSteal under $\langle \mathcal{M}^B, \mathcal{D}_{\text{aux}}^P \rangle$, MemInf and AttrInf under $\langle \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$, MemInf and AttrInf under $\langle \mathcal{M}^W, \mathcal{D}_{\text{aux}}^P \rangle$, MemInf and ModInv under $\langle \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$, and AttrInf and ModInv under $\langle \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$.

Figure 10 shows that there is a strong negative correlation between membership inference and model stealing ($\langle \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$) with respect to their performance ($r = -0.90$). Specifically, worse membership inference corresponds to better model stealing. This follows from the discussion around overfitting (Section 6.3). We also observe a strong negative correlation between membership inference and model inversion, except for FMNIST.

On the other hand, there does not seem to be any clear relation between attribute inference and model inversion, as well as between membership inference and attribute inference.

7 Defenses

We now evaluate two representative defense mechanisms, namely differential privacy (DP) and Knowledge Distillation (KD), and investigate whether or not, and how effectively, they can be used to mitigate these attacks.

7.1 Techniques

First, we introduce the concepts of DP and KD.

7.1.1 Differential Privacy (DP)

Differential privacy (DP) [11, 24] guarantees that any single data sample in a dataset has a limited impact on the output.

Definition 1 ((ϵ, δ) -DP). A randomization algorithm \mathcal{A} satisfies (ϵ, δ) -differential privacy, with $\epsilon > 0$ and $0 \leq \delta < 1$, if and only if for any two neighboring datasets D and D' that differ in one record, we have:

$$\forall T \subseteq \text{Range}(\mathcal{A}) : \Pr[\mathcal{A}(D) \in T] \leq e^\epsilon \Pr[\mathcal{A}(D') \in T] + \delta,$$

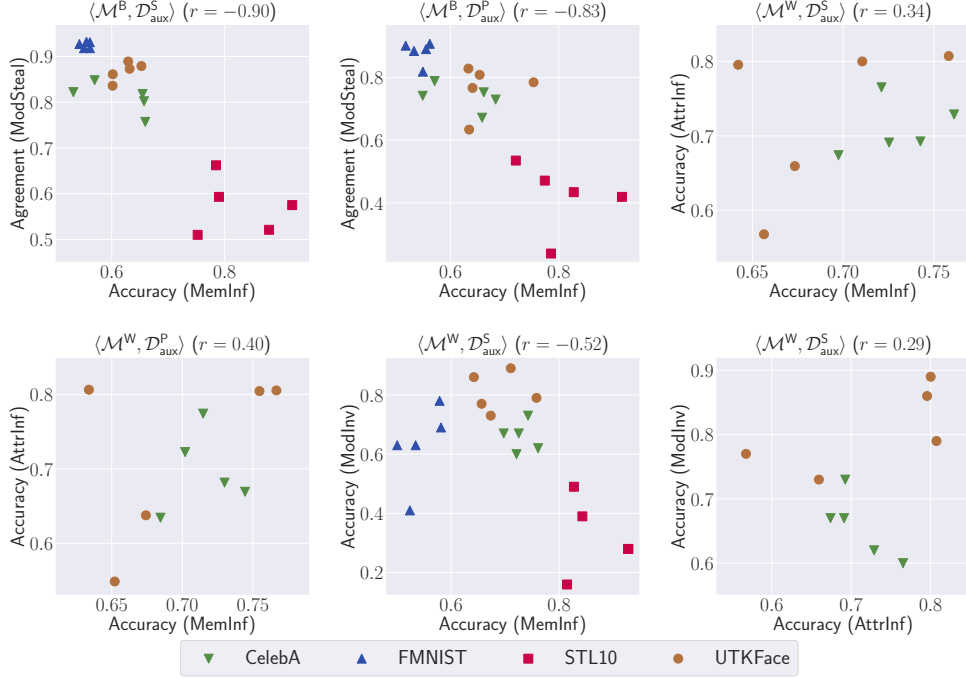


Figure 10: The relation between different attacks under the same threat model.

	CelebA			FMNIST			STL10			UTKFace		
	Original	$\epsilon_1=5.14$	$\epsilon_2=6.57$	Original	$\epsilon_1=8.41$	$\epsilon_2=9.36$	Original	$\epsilon_1=8.83$	$\epsilon_2=9.60$	Original	$\epsilon_1=9.58$	$\epsilon_2=7.76$
$\langle \text{MemInf}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$	0.66	0.50	0.50	0.56	0.50	0.50	0.78	0.49	0.50	0.63	0.50	0.50
$\langle \text{MemInf}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^P \rangle$	0.66	0.50	0.50	0.56	0.50	0.50	0.72	0.50	0.50	0.63	0.50	0.50
$\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$	0.72	0.50	0.50	0.58	0.50	0.50	0.84	0.54	0.54	0.64	0.50	0.50
$\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^P \rangle$	0.71	0.50	0.50	0.58	0.51	0.50	0.84	0.52	0.53	0.63	0.48	0.50
$\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^N \rangle$	0.06	0.06	0.06	0.98	0.99	0.99	0.20	0.20	0.20	0.07	0.07	0.07
$\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$	0.60	0.59	0.57	0.69	0.54	0.57	0.39	0.17	0.32	0.86	0.62	0.75
$\langle \text{ModSteal}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$	0.82	0.90	0.89	0.93	0.93	0.92	0.66	0.53	0.51	0.87	0.79	0.85
$\langle \text{ModSteal}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^P \rangle$	0.75	0.87	0.87	0.91	0.92	0.92	0.54	0.48	0.47	0.83	0.77	0.82
$\langle \text{AttrInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$	0.77	0.73	0.70	-	-	-	-	-	-	0.80	0.72	0.78
$\langle \text{AttrInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^P \rangle$	0.77	0.73	0.71	-	-	-	-	-	-	0.81	0.74	0.77

Table 3: Attack performance under different threat models and datasets, on SimpleCCN, using DP-SGD. For MemInf, ModInv, and AttrInf, we use accuracy, for ModSteal, agreement.

where $\text{Range}(\mathcal{A})$ denotes the set of all possible outputs of the algorithm \mathcal{A} , δ can be interpreted as the probability that the mechanism fail to satisfy ϵ -DP.

Gaussian Mechanism. There are several approaches to design mechanisms satisfying (ϵ, δ) -differential privacy. The Gaussian mechanism is arguably the most widely used one in the ML context. Essentially, it computes a function f on dataset D by adding random (Gaussian) noise to $f(D)$. The magnitude of the noise depends on Δ_f , i.e., the *global sensitivity* of f (also referred to as the ℓ_2 sensitivity). More formally, we define the \mathcal{A} mechanism as

$$\mathcal{A}(D) = f(D) + \mathcal{N}(0, \Delta_f^2 \sigma^2 \mathbf{I})$$

where $\Delta_f = \max_{(D, D'): D \sim D'} \|f(D) - f(D')\|_2$.

Here, $\mathcal{N}(0, \Delta_f^2 \sigma^2 \mathbf{I})$ denotes a multi-dimensional random variable sampled from the normal distribution with mean 0 and standard deviation $\Delta_f \sigma$, and $\sigma = \sqrt{2 \ln \frac{1.25}{\delta}} / \epsilon$.

DP-SGD. We experiment with Differentially-Private Stochastic Gradient Descent (DP-SGD) [1], the most representative DP mechanism for protecting machine learning models. In general, DP-SGD adds Gaussian noise to gradient g during the target ML model’s training process, i.e., $\tilde{g} = g + \mathcal{N}(0, \Delta_f^2 \sigma^2 \mathbf{I})$. Due to the unbounded nature of the gradient of ML models, one needs to first clip the gradient before adding noise. Concretely, we can bound the ℓ_2 norm of the gradient to C by calculating $g \leftarrow g / \max\{1, \|g\|_2 / C\}$.

Composition. Note that we need to calculate the gradient multiple times when training an ML model. Each calculation requires access to the training data and thus consumes a por-

tion of the privacy budget. We use the notion of zCDP [3] to calculate the total privacy budget consumption. The general idea of zCDP is to connect (ϵ, δ) -DP to Rényi divergence, and use the properties of Rényi divergence to achieve tighter composition property.

7.1.2 Knowledge Distillation (KD)

Another defense mechanism we consider is Knowledge Distillation (KD) [20]. Generally, KD aims to transfer the knowledge from a larger model (original model) to a smaller model (distilled model). Compared to the original model, the distilled model has a lower capacity, which may make it remember less information about its training data.

Papernot et al. [40] show that KD can reduce the risks of machine learning models against adversarial examples. Here, we take a broader view investigating whether or not KD is effective to defend against inference attacks.

7.2 Experimental Setup

Both DP-SGD and KD are applied in the training process of target models. Due to space limitations, we only apply DP-SGD to SimpleCNN and KD to VGG19.

DP-SGD Target Model. We use the Opacus library⁵ to implement DP-SGD on SimpleCNN. This allows a user to configure the clip bound C , the standard deviation of the Gaussian noise σ , and the failure probability δ , then the library can automatically calculate the total privacy budget ϵ using zCDP. A larger number of epochs implies higher ϵ . Our target model is trained for 300 epochs, thus we fix $\delta=1e-5$ and choose two sets of C and σ such that ϵ is smaller than 10. We list these settings in the second row of Table 3. All the other hyperparameters are the same as presented in Section 5.3.

Distillation Target Model. We distill the model knowledge of VGG19 (16 convolution layers and 3 fully connected layers) to a smaller model, i.e., VGG11 [47] (8 convolution layers and 3 fully connected layers). We use Kullback-Leibler divergence as the soft target loss, namely the distill loss, with the temperature set to 20. For the student loss, i.e., the hard loss, we use cross-entropy. We set α to 0.7 for the ratio of the soft target loss. Other settings are the same as the target model’s training phase in Section 5.3.

7.3 Results

DP-SGD. Table 3 reports the performance of inference attacks against target models protected by DP-SGD. For MemInf, DP-SGD is effective in almost all cases. For instance, for $\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{aux}^S \rangle$ on the CelebA dataset, the accuracy of membership inference drops from 0.72 to 0.50, which is the random guess. This is expected as DP, by definition, can mitigate membership inference. For ModInv and AttrInf, DP-SGD can only reduce the attack accuracy to a small extent. However, the MSE loss for $\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{aux}^N \rangle$ remains stable.

DP-SGD indeed reduces the risks of model stealing on STL10 and UTKFace under different threat models. For instance, for $\langle \text{ModSteal}, \mathcal{M}^B, \mathcal{D}_{aux}^S \rangle$ on STL10, the agreement for the two different privacy budgets are 0.53 and 0.51, while the agreement for the original model is 0.66. Meanwhile, DP-SGD does not influence model stealing on FMNIST. Interestingly, it actually enhances the performance of model stealing on CelebA. Overall, DP-SGD can effectively defend against membership inference attacks, but not the others.

KD. In Table 4, we report the effectiveness of KD as a general defense mechanism. We do not observe any significant decrease in attack performance for model inversion, attribute inference, and model stealing on original vs. the distilled models. Specifically, the attack performance difference, in most cases, is less than 5%. In certain cases, KD is effective against membership inference, but to a lesser extent compared to DP-SGD. For instance, the performance of $\langle \text{MemInf}, \mathcal{M}^B, \mathcal{D}_{aux}^S \rangle$ on the STL10 dataset drops from 0.79 to 0.65.

Effect on Utility. Finally, we measure how much defenses reduce the performance of the target models on their original tasks; see Table 5. We observe that DP-SGD reduces the target model’s performance, but to a small extent. For instance, the testing accuracy of SimpleCNN with DP-SGD on CelebA under ϵ_1 and ϵ_2 is 0.65 and 0.67, respectively, while the original testing accuracy is 0.71. KD only has a very minor influence on model utility; however, as discussed above, that is not an overall effective defense mechanism against inference attacks.

8 Related Work

We now review relevant related work on inference attacks and defenses, as well as software dedicated to evaluating them.

Membership Inference Attacks. Shokri et al. [46] propose the first membership inference attack against black-box ML models: they train multiple shadow models to simulate the target model and use multiple attack models to conduct the inference. Salem et al. [44] later relax several key assumptions from [46]; namely, using multiple shadow models, the knowledge of the target model structure, and having a dataset from the same distribution as the target model’s. Yeom et al. [55] assume that the adversary knows the target model’s training dataset’s distribution and size, and they collude with the training algorithm. Both [44] and [55] are close in performance to Shokri et al.’s attacks [46]. In this paper, we implement the attack proposed by Salem et al. [44], i.e., one shadow model, one attack model, and a shadow dataset.

More recently, researchers have generalized membership inference to other settings, including natural language processing models [5, 49], generative models [6, 16, 19], and federated learning [28, 31]. Note that previous work [44, 46] also shows that overfitting is the major factor causing membership inference risks. To the best of our knowledge, however, none of them has investigated other factors studied in our paper, such as the influence of dataset complexity or the relationship among different inference attacks.

⁵<https://github.com/pytorch/opacus>

	CelebA		FMNIST		STL10		UTKFace	
	Original	Distilled	Original	Distilled	Original	Distilled	Original	Distilled
$\langle \text{MemInf}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$	0.53	0.58	0.56	0.52	0.79	0.65	0.63	0.61
$\langle \text{MemInf}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^P \rangle$	0.55	0.57	0.52	0.55	0.77	0.70	0.65	0.55
$\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$	0.70	0.65	0.53	0.52	0.81	0.78	0.66	0.59
$\langle \text{MemInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^P \rangle$	0.68	0.69	0.55	0.57	0.83	0.79	0.65	0.61
$\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^N \rangle$	0.06	0.06	0.99	0.99	0.20	0.20	0.07	0.07
$\langle \text{ModInv}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$	0.67	0.60	0.63	0.61	0.16	0.23	0.77	0.67
$\langle \text{ModSteal}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^S \rangle$	0.82	0.79	0.93	0.94	0.59	0.61	0.89	0.88
$\langle \text{ModSteal}, \mathcal{M}^B, \mathcal{D}_{\text{aux}}^P \rangle$	0.74	0.74	0.90	0.92	0.47	0.51	0.81	0.81
$\langle \text{AttrInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^S \rangle$	0.67	0.68	-	-	-	-	0.57	0.57
$\langle \text{AttrInf}, \mathcal{M}^W, \mathcal{D}_{\text{aux}}^P \rangle$	0.63	0.65	-	-	-	-	0.55	0.59

Table 4: Attack performance under different threat models and datasets, on VGG19, using Knowledge Distillation (KD). For MemInf, ModInv, and AttrInf, we use accuracy, for ModSteal, agreement.

Experiment	Model	CelebA	FMNIST	STL10	UTKFace
DP-SGD (ϵ_1)	SimpleCNN	0.65	0.83	0.35	0.70
DP-SGD (ϵ_2)	SimpleCNN	0.67	0.84	0.31	0.68
KD	VGG19	0.71	0.92	0.59	0.82
No Defense	SimpleCNN	0.71	0.90	0.52	0.82
No Defense	VGG19	0.73	0.91	0.59	0.83

Table 5: Performance of target models protected by DP-SGD and KD.

Attribute Inference. Prior research [2, 14] has studied macro-level attribute inference attacks against ML models, whereby the adversary aims to infer some general properties of the training dataset. Melis et al. [28] propose the first sample-level attribute inference attack against federated machine learning systems. Song and Shmatikov [50] reveal that the risks of attribute inference are caused by the intrinsic overlearning characteristics of machine learning models.

Model Inversion. Model inversion is first proposed by Fredrikson et al. [13] in the setting of drug dose classification. Later, they extend model inversion to general ML settings relying on back-propagation over a target ML model’s parameters [12]. More recently, Zhang et al. [56] develop a more advanced attack aiming to synthesize the training dataset relying on GANs. Finally, Carlini et al. [4] show that model inversion can be effectively performed against natural language processing models as well.

Model Stealing. Tramèr et al. [51] propose the first model stealing attack against black-box machine learning API. Orekondy et al. [34] develop a reinforcement learning based framework to optimize both query time and effectiveness. Also, Wang and Gong [52] and Oh et al. [33] show that hyperparameters of a target model can be inferred as well.

Defense Mechanisms. A few defense mechanisms have been proposed to mitigate membership inference attacks [21, 30, 44]. However, these defenses are specifically designed for membership inference and cannot mitigate other inference attacks. For instance, Salem et al. [44] propose to reduce overfitting of the target model as a defense, however, as

we show in our analysis (see Section 6.3), reducing overfitting will improve the performance of model stealing.

Differential privacy (DP) [11, 24] guarantees that any single data sample in a dataset has a limited impact on the output of an algorithm. As such, it is an effective defense mechanism against inference attacks. Abadi et al. [1] introduce DP-SGD, which adds Gaussian noise to the gradients of the target model during the training process. Another DP method for protecting the privacy of ML models is PATE [36]: a set of teacher models is trained on a private dataset, which are used to label a public dataset in a differentially private manner. The final public dataset is then used to train a student model. Recently, Nasr et al. [32] instantiate a number of attacks against ML to evaluate the effectiveness of DP defenses and in particular how tight are theoretical DP bounds.

Another defense mechanism is Knowledge Distillation (KD) [20]. Papernot et al. [40] propose a defensive distillation mechanism to effectively reduce the risks for target models with respect to adversarial examples. Shejwalkar and Houmansadr [45] reveal that distillation can reduce the gap between the posteriors of members and non-members, thus protecting membership privacy. In our experiments, we show that distillation is indeed effective against certain target models supported by ML-DOCTOR, however, it cannot defend other types of inference attacks.

Risk Assessment Tools. Finally, researchers have recently developed a number of software tools to measure the potential security/privacy risks of ML models. Ling et al. [26] propose DEEPSEC, a security analysis system to evaluate different adversarial example attacks and defenses. Another system for adversarial examples is CleverHans [37]. Pang et al. [35] introduce TROJANZOO, which focuses on backdoor attacks.

Closer to our work is ML Privacy Meter [29], which jointly considers membership inference attacks in both black-box and white-box settings. Unlike ML Privacy Meter, which focuses on membership inference only, ML-DOCTOR considers four types of inference attacks simultaneously. In addition, we rely on ML-DOCTOR to perform a comprehensive analysis for all these inference attacks.

9 Conclusion

In this paper, we performed the first holistic analysis of privacy risks caused by inference attacks against machine learning models. We established a taxonomy of threat models for four types of inference attacks including membership inference, model inversion, attribute inference, and model stealing. We conducted an extensive measurement study, over five model architectures and four datasets, of both attacks and defenses. Among other things, we found that the complexity of the training dataset plays an important role in the attack’s performance, while the effectiveness of model stealing and membership inference attacks are negatively correlated. We also showed that defenses such as DP-SGD and Knowledge Distillation can only hope to mitigate some of the inference attacks.

We integrated all the attacks and defenses into a re-usable, modular software called ML-DOCTOR. We envision that ML-DOCTOR can be used in various scenarios. An ML model owner can use ML-DOCTOR to evaluate the model’s inference risks before deploying it in the real world. We are also confident that, as we will make all source code publicly available, ML-DOCTOR will serve as a benchmark tool to facilitate future research on inference attacks and defenses.

Currently, ML-DOCTOR concentrates on classification models, as classification is the most popular ML application and most of the current inference attacks are run on ML classifiers. Recently, researchers have demonstrated that inference attacks can also be successfully launched on other types of ML models, such as language models [48, 49], generative models [6, 16], and graph-based models [18], as well as other training paradigms, such as federated learning [28]. We plan to extend ML-DOCTOR to support a broader range of ML application scenarios.

Finally, while ML-DOCTOR is designed for inference attacks, we plan to integrate tools [26, 35, 37] geared to evaluate risks aimed to jeopardize models’ functionality, e.g., adversarial example, data poisoning, etc., thus providing a one-stop-shop toward enabling secure and trustworthy AI.

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